

Square Root of a Variable

If a is a positive real number and m is an even integer, then $\sqrt{a^m} = a^{\frac{m}{2}}$ Remember: $a^{\frac{\text{power}}{\text{root}}}$

$$\sqrt{a^6} = a^{\frac{6}{2}} = a^3$$

$$\sqrt{z^{36}} = z^{\frac{36}{2}} = z^{18} \text{ CAUTION: It is very tempting to take the square root of 36 and answer incorrectly } z^6$$

If m is an odd integer, rewrite m as the sum of a multiple of 2 and 1.

$$\sqrt{a^7} = \sqrt{a^{6+1}} = \sqrt{a^6} \sqrt{a} = a^3 \sqrt{a}$$

$$\sqrt{a^{15}} = \sqrt{a^{14+1}} = \sqrt{a^{14}} \sqrt{a} = a^7 \sqrt{a}$$

TRY:

$$\sqrt{n^5}$$

$$\sqrt{z^9}$$

Combinations:

$$\sqrt{12x^{11}} = \sqrt{3 \cdot 4 \cdot x^{10} \cdot x} = 2x^5 \sqrt{3x}$$

TRY:

$$\sqrt{12x^8}$$

$$\sqrt{36n^2}$$

$$\sqrt{3n^3}$$

$$\sqrt{8z^{16}}$$