

Lesson 08: Proportions and Percents

Proportions

Vocabulary

Proportion	An equation that compares two equal fractions (or rates) Ex: $\frac{3}{5} = \frac{6}{10}$ is read "3 is to 5 as 6 is to 10"
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TRY: Write the proportions.

5 is to 18 as 15 is to 54

$$\frac{\square}{\square} = \frac{\square}{\square}$$

4 is to 12 as 20 is to 60

$$\frac{\square}{\square} = \frac{\square}{\square}$$

Is this the same as:

If it takes 4 minutes to fold 12 books, working at the same rate, it will take 20 minutes to fold 60 books.

A proportion is known to be true if the **cross product**, the product of the **extremes** equals the product of the **means**.

$$\text{That is, } \frac{3}{5} = \frac{6}{10} \text{ when } 3 \cdot 10 = 5 \cdot 6$$

extremes = means

Extremes–Means Property.

$$\text{If } \frac{a}{b} = \frac{c}{d}, \text{ then } ad = bc \text{ provided that } b \neq 0 \text{ and } d \neq 0.$$

TRY: Determine whether each pair of fractions is equivalent.

$$\frac{3}{7} = \frac{27}{63}$$

$$\frac{4}{5} = \frac{3}{4}$$

$$\frac{5}{1} = \frac{200}{10}$$

TRY: Use the extremes = means rule to find the value of x .

$$\frac{6}{7} = \frac{x}{56}$$

$$\frac{3}{8} = \frac{5}{x}$$

$$\frac{2}{5} = \frac{10}{x}$$

$$\frac{0.8}{x} = \frac{5}{40}$$

Proportion Problems

If 5 feet of rope costs \$2.10, what would 7 feet of rope cost?

This problem can be thought of in two ways:

$$\frac{5}{7} = \frac{2.10}{x} \quad \text{OR} \quad \frac{5}{2.10} = \frac{7}{x} \quad \text{Either way, } 5x = 7(2.10)$$

TRY:

If 12 apples cost \$4.80, what would 5 apples cost?

JJ worked 2.4 hours and received \$8.64. If KT works 10 hours at the same rate of pay, how much will KT receive?

The paint machine can paint 30 signs in 2 minutes. How many signs can be painted in 4 hours?